

MATHEMATICS LECTURES FOR IIT-JEE BY MANISH KALIA

TOPIC –PERMUTATIONS AND COMBINATIONS

JEE-MAINS (PREVIOUS YEAR)

MCQ-Single Correct

1. A man X has 7 friends, 4 of them are ladies and 3 are men. His wife Y also has 7 friends, 3 of them are ladies and 4 are men. Assume X and Y have no common friends. Then the total number of ways in which X and Y together can throw a party inviting 3 ladies and 3 men, so that 3 friends of each of X and Y are in this party, is :
- (1) 485 (2) 468
(3) 469 (4) 484 [2017]
2. If all the words (with or without meaning) having five letters, formed using the letters of the word SMALL and arranged as in a dictionary; then the position of the word SMALL is :
- (1) 59th (2) 52nd
(3) 58th (4) 46th [2016]
3. The number of points, having both co-ordinates as integers, that lie in the interior of the triangle with vertices (0,0) , (0,41) and (41,0), is :
- (1) 861 (2) 820
(3) 780 (4) 901 [2015]
4. The number of integers greater than 6,000 that can be formed, using the digits 3, 5, 6, 7 and 8, without repetition, is :
- (1) 192 (2) 120
(3) 72 (4) 216 [2015]
5. Let T_n be the number of all possible triangles formed by joining vertices of an n-sided regular polygon. If $T_{n+1} - T_n = 10$, then the value of n is
- (1) 5 (2) 10
(3) 8 (4) 7 [2013]

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6. Assuming the balls to be identical except for difference in colours, the number of ways in which one or more balls can be selected from 10 white, 9 green and 7 black balls is
- (1) 630 (2) 879
(3) 880 (4) 629 [2012]
7. Let $X = \{1, 2, 3, 4, 5\}$. The number of different ordered pairs (Y, Z) that can be formed such that $Y \subseteq X$, $Z \subseteq X$, and $Y \cap Z$ is empty, is
- (1) 2^5 (2) 5^3
(3) 5^2 (4) 3^5 [2012]
8. There are 10 points in a plane, out of these 6 are collinear. If N is the number of triangles formed by joining these points, then
- (1) $140 < N \leq 190$ (2) $N > 190$
(3) $N \leq 100$ (4) $100 < N \leq 140$ [2011]
9. From 6 different novels and 3 different dictionaries, 4 novels and 1 dictionary are to be selected and arranged in a row on the shelf so that the dictionary is always in the middle. Then the number of such arrangements is
- (1) less than 500 (2) at least 500 but less than 750
(3) at least 750 but less than 1000 (4) at least 1000 [2009]
10. How many different words can be formed by jumbling the letters in the word MISSISSIPPI in which no two S are adjacent?
- (1) $8 \cdot {}^6C_4 \cdot {}^7C_4$ (2) $6 \cdot 7 \cdot {}^8C_4$
(3) $6 \cdot 8 \cdot {}^7C_4$ (4) $7 \cdot {}^6C_4 \cdot {}^8C_4$ [2008]
11. The set $S = \{1, 2, 3, \dots, 12\}$ is to be partitioned into three sets A, B, C of equal size. Thus, $A \cup B \cup C = S$, $A \cap B = B \cap C = A \cap C = \phi$. The number of ways to partition S is
- (1) $\frac{12!}{3!(4!)^3}$ (2) $\frac{12!}{3!(3!)^4}$

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- (3) $\frac{12!}{(4!)^3}$ (4) $\frac{12!}{(3!)^4}$ [2007]
12. At an election, a voter may vote for any number of candidates, not greater than the number to be elected. There are 10 candidates and 4 are to be elected. If a voter votes for at least one candidate, then the number of ways in which he can vote is
- (1) 5040 (2) 6210
(3) 385 (4) 1110 [2006]
13. If the letters of word SACHIN are arranged in all possible ways and these words are written out as in dictionary, then the word SACHIN appears at serial number
- (1) 601 (2) 600
(3) 603 (4) 602 [2005]
14. How many ways are there to arrange the letters in the word GARDEN with the vowels in alphabetic order?
- (1) 120 (2) 480
(3) 360 (4) 240 [2004]
15. The number of ways of distributing 8 identical balls in 3 distinct boxes so that none of the boxes is empty is
- (1) 5 (2) 8C_3
(3) 3^8 (4) 21 [2004]
16. A student is to answer 10 out of 13 questions in an examination such that he must choose at least 4 from the first five questions. The number of choices available to him is
- (1) 140 (2) 196
(3) 280 (4) 346 [2003]
17. The number of ways in which 6 men and 5 women can dine at a round table if no two women are to sit together is given by
- (1) $6! \times 5!$ (2) 30

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- (3) $5! \times 4!$ (4) $7! \times 5!$ [2003]
18. If ${}^n C_r$ denotes the number of combinations of n things taken r at a time, then the expression ${}^n C_{r+1} + {}^n C_{r-1} + 2 \times {}^n C_r$ equals
- (1) ${}^{n+2} C_r$ (2) ${}^{n+2} C_{r+1}$
(3) ${}^{n+1} C_r$ (4) ${}^{n+1} C_{r+1}$ [2003]
19. If $f(x) = x^n$, then the value of $f'(1) - \frac{f''(1)}{2!} + \frac{f'''(1)}{3!} - \dots + \frac{(-1)^n f^{(n)}(1)}{n!}$ is
- (1) 2^n (2) 2^{n-1}
(3) 0 (4) 1 [2003]
20. Number of numbers greater than 1000 but less than 4000 formed using the digits 0, 2, 3, 4 with repetition allowed is
- (1) 125 (2) 105
(3) 128 (4) 625 [2002]
21. Five digit number divisible by 3 is formed using 0, 1, 2, 3, 4, 6 and 7 without repetition. Total number of such numbers are
- (1) 312 (2) 3125
(3) 120 (4) 216 [2002]
22. The sum of integers from 1 to 100 that are divisible by 2 or 5 is
- (1) 3000 (2) 3050
(3) 3600 (4) 3250 [2002]
23. Total number of four digit odd numbers that can be formed using 0, 1, 2, 3, 5, 7 are
- (1) 216 (2) 375
(3) 400 (4) 720 [2002]

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Assertion – Reason Type

1. In a shop there are five types of ice-creams available. A child buys six ice-creams.

Statement – I : The number of different ways the child can buy the six ice-creams is ${}^{10}C_5$.

Statement – II : The number of different ways the child can buy the six ice-creams is equal to the number of different ways of arranging 6 A's and 4 B's in a row.

ALPHA CLASSES